MATH 100—Homework 06

Due: Friday April 26

NAME _

Directions: please print this page, and put your solutions in the space provided. If you need extra space, you can attach another sheet of paper.

1. Let
$$A = \begin{bmatrix} 2 & 3 \\ 4 & 1 \end{bmatrix}$$
.

(a) Show that the eigenvalues of A are $\lambda = -2, 5$ using the characteristic polynomial.

(b) Show that A is diagonalizable by finding a diagonal matrix D and an invertible matrix P such that $A = PDP^{-1}$. Please show all work.

D =

2. Let
$$B = \begin{bmatrix} 4 & 0 & 0 \\ 2 & 5 & 4 \\ 0 & 0 & 5 \end{bmatrix}$$
.

(a) Show that the eigenvalues of B are $\lambda = 4, 5$ (5 has multiplicity 2) using the characteristic polynomial.

(b) Show that B is not diagonalizable. Please show all work and explain your reasoning.