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## Worksheet 17

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1. The graph of $f(x)$ is below.

(a) On what intervals is $f$ increasing?
(d) On what intervals is $f$ concave up?
(b) On what intervals is $f$ decreasing?
(e) On what intervals is $f$ concave down?
(c) For which $x$-values is there a local extrema?
(f) For which $x$-values is there an inflection point?
2. Draw the graph of a function $f$ that has the given properties:

- $f$ is continuous everywhere except at $x=4$
- $f^{\prime}(x)<0$ only when $3<x<4$,
- $f^{\prime \prime}(x)>0$ only when $0<x<2$
- $\lim _{x \rightarrow \infty} f(x)=1$

(a) For which $x$-values is there a local extrema?
(b) For which $x$-values is there an inflection point?

3. Let $f(x)=x^{4} e^{-x}$. Find all intervals of increasing or decreasing, all intervals where the graph is concave up or concave down, all local extrema, and all inflections points. (Your answers go below.) Also, use this information to sketch the graph of $y=f(x)$.

- On what intervals is $f$ increasing?
- On what intervals is $f$ decreasing?
- For which $x$-values is there a local extrema?
- On what intervals is $f$ concave up?
- On what intervals is $f$ concave down?
- For which $x$-values is there an inflection point?


