

MATH 31, LECTURE 10

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For emphasis:

To calculate volumes:

- (1) Draw the picture (very important!!!!). Can you “fill the solid” with parallel discs/washers/(other cross-sections with easily-computable areas)? Can you “fill the solid” with cylindrical shells?
- (2) Washers: Find the inner radius and outer radius for each washer. (If the inner radius is zero, it’s a disc.) Shells: Find the radius, circumference, and height.
- (3) Use the formula to set up the integral. (Hopefully you will get to the point where you don’t have to memorize the formula—it just makes sense.)
- (4) Evaluate the integral.

Example. The region bounded by $x = 0$, $y = 0$, $y = \cos x$ for $0 \leq x \leq \frac{\pi}{2}$, rotated about the y -axis. Set up the integral for the volume. Using Integration by Parts (§7.1) we find that, using the washer method or the shell method, the volume is $\pi^2 - 2\pi$.

Someone asked about the problem

$$\int_0^1 x\sqrt{1-x^4} dx$$

from Section 5.5.

Evil Test Question. Evaluate the integral

$$\int_0^1 (x+1)^{12} dx.$$

The easiest way is to use the Chain Rule/ the Substitution Rule.

I also answered other questions; I don’t remember what exactly.