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Group Work 18

1. Find the following limits.

(a) $\lim_{x \rightarrow 1} \frac{x \sin(x-1)}{2x^2 - x - 1}$

(b) $\lim_{x \rightarrow \pi} \frac{1 + \cos x}{1 - \cos x}$

(c) $\lim_{x \rightarrow -\infty} x^2 e^x$

(d) $\lim_{x \rightarrow 0^-} \left(\frac{1}{x} - \frac{1}{e^x - 1} \right)$

2. Consider the limit $\lim_{x \rightarrow 0^+} (\cos x)^{1/x^2}$.

(a) What does “direct substitution” yield for the limit $\lim_{x \rightarrow 0^+} (\cos x)^{1/x^2}$?

(b) Find $\lim_{x \rightarrow 0^+} (\cos x)^{1/x^2}$ by using logarithms.

i. “Take \ln ” of both sides of $y = (\cos x)^{1/x^2}$ and use rules of logs to simplify.

ii. Take the limit as $x \rightarrow 0^+$ of your answer to the previous part to find $\lim_{x \rightarrow 0^+} \ln y$.

iii. Exponentiate your answer to the previous part to get your final answer for $\lim_{x \rightarrow 0^+} y$.