

15 – Inverse Trig & Logs

Theorem: Derivatives of the Inverse Trigonometric Functions

- $(\arcsin x)' = (\sin^{-1} x)' = \frac{1}{\sqrt{1-x^2}}$
- $(\arccos x)' = (\cos^{-1} x)' = -\frac{1}{\sqrt{1-x^2}}$
- $(\arctan x)' = (\tan^{-1} x)' = \frac{1}{1+x^2}$
- $(\operatorname{arccot} x)' = (\cot^{-1} x)' = -\frac{1}{1+x^2}$
- $(\operatorname{arcsec} x)' = (\sec^{-1} x)' = \frac{1}{x\sqrt{x^2-1}}$
- $(\operatorname{arccsc} x)' = (\csc^{-1} x)' = -\frac{1}{x\sqrt{x^2-1}}$

Theorem: Derivatives of Logarithmic Functions

- $(\ln x)' = \frac{1}{x}$
- $(\ln |x|)' = \frac{1}{x}$
- $(\log_a x)' = \frac{1}{x \ln a}$

1. Find the derivative.

(a) $y = \frac{\arcsin(1-x)}{\ln(x^5)}$

(b) $y = \ln(\arctan(x^3) \log_3(x))$

(c) $e^{2x}y = \ln(y^3)$

2. Consider the function $f(x) = x^{\sin x}$.

(a) A classmate tells you that $f'(x) = (\sin x)x^{(\sin x)-1}$. What are they thinking? What is the error?

(b) Find $f'(x)$ by using **logarithmic differentiation**.