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## 19 - Max \& Min Values

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## Definition: Absolute (or Global) Extrema

Let $f$ be a function with domain $D$. Suppose $c$ is in $D$.

1. $f(c)$ is called the absolute minimum value of $f$ on $D$ if $f(c) \leq f(x)$ for all $x$ in $D$.
2. $f(c)$ is called the absolute maximum value of $f$ on $D$ if $f(c) \geq f(x)$ for all $x$ in $D$.
3. The graph of $f(x)$ is below. Find each of the following.

(a) The absolute min value for $f$ on $[-3,5]$ ?
(b) The absolute max value for $f$ on $[-3,5]$ ?
(c) The absolute min value for $f$ on $[0,3.5]$ ?
(d) The absolute max value for $f$ on $[0,3.5]$ ?
(e) The absolute min value for $f$ on $(0,3.5)$ ?
(f) The absolute max value for $f$ on $(0,3.5)$ ?
(g) The absolute min value for $f$ on $(-\infty, \infty)$ ?
(h) The absolute max value for $f$ on $(-\infty, \infty)$ ?

Let $f$ be a function.

1. $f(c)$ is called a local minimum value of $f$ on $D$ if $f(c) \leq f(x)$ for all $x$ near $c$.
2. $f(c)$ is called a local maximum value of $f$ on $D$ if $f(c) \geq f(x)$ for all $x$ near $c$.
3. Let $f(x)$ be the same as in the previous problem.
(a) Find all local minimum values of $f$.
(b) Find all local maximum values of $f$.
4. Sketch the graph of $f$, and find all absolute and local extrema on its domain.
$f(x)= \begin{cases}x^{2} & \text { if }-2 \leq x \leq 1 \\ -x+2 & \text { if } x>1\end{cases}$

Abs. max:
Local max's:
Abs. min:
Local min's:

4. Explain why $f(x)=e^{x}$ has no absolute minimum value on $(-\infty, \infty)$.
5. Explain why $g(x)=x^{2}$ has no absolute maximum value on $(-1,2)$.

## Theorem: Extreme Value Theorem

If $f$ is continuous on a closed interval $[a, b]$, then $f$ has both an absolute max and min on $[a, b]$.

