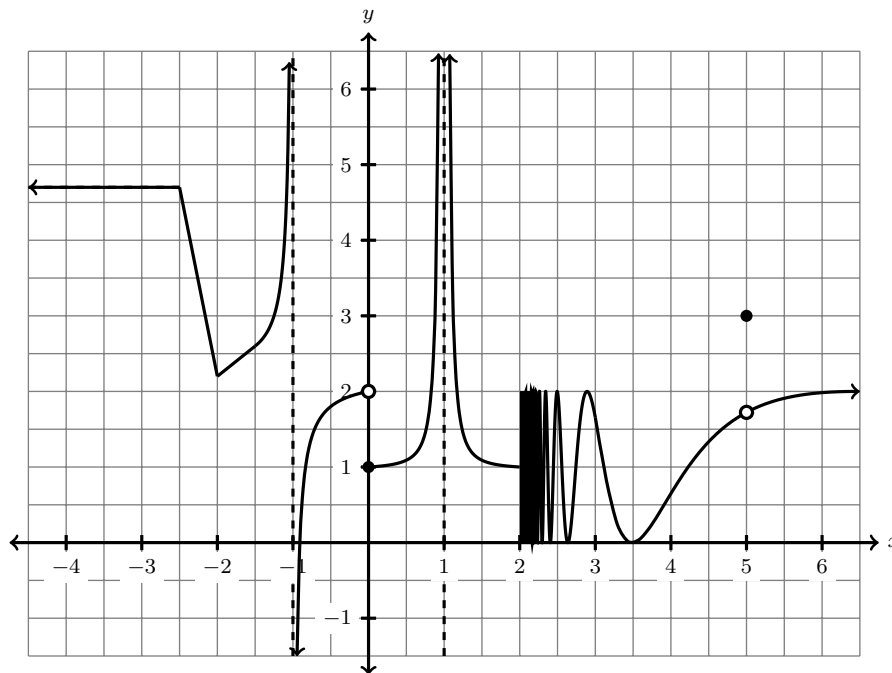


# 06 – Continuity

## Definition: Continuity

A function  $f$  is **continuous at a number**  $a$  if  $\lim_{x \rightarrow a} f(x) = f(a)$ , and both sides exist.

1. Suppose the graph of  $y = f(x)$  is given below. Find all  $x$ -values where  $f$  is discontinuous.



Discontinuous at  $x =$  \_\_\_\_\_

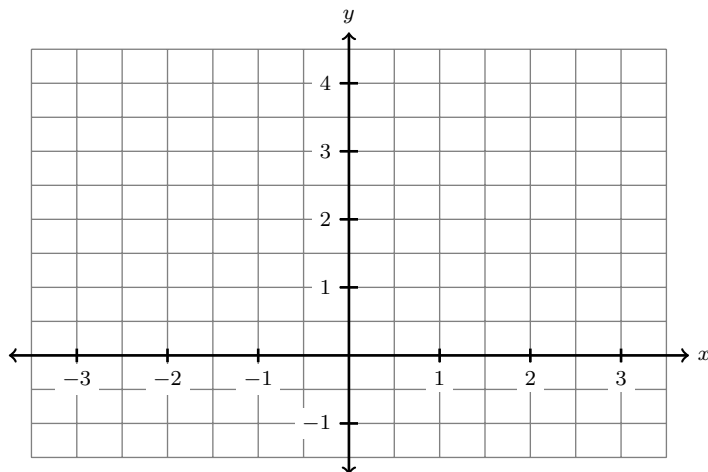
## Definition: One-sided Continuity

- A function  $f$  is **continuous from the left** at  $a$  if  $\lim_{x \rightarrow a^-} f(x) = f(a)$ , and both sides exist.
- A function  $f$  is **continuous from the right** at  $a$  if  $\lim_{x \rightarrow a^+} f(x) = f(a)$ , and both sides exist.

2. For the graph of  $f$  above, determine if  $f$  is continuous from the left, from the right, both, or neither at each of  $x = -2, 0, 1$ .

3. Sketch the graph of  $y = f(x)$  (defined below), and find all values for  $x$  where  $f$  is discontinuous.

$$f(x) = \begin{cases} x + 1 & \text{if } x < 0 \\ e^x & \text{if } 0 \leq x \leq 1 \\ 2 - x & \text{if } x > 1 \end{cases}$$



Discontinuous at  $x =$  \_\_\_\_\_

4. For what value of the constant  $c$  is the function  $f$  continuous on  $(-\infty, \infty)$ ?

$$f(x) = \begin{cases} cx^2 + 2x & \text{if } x < 2 \\ x^3 - cx & \text{if } x \geq 2 \end{cases}$$

$f$  is continuous provided  $c =$  \_\_\_\_\_

5. *True or False:* the function  $f(x) = \tan(x)$  is continuous on its domain. Make sure to explain!