

# 05 – Limits Algebraically

## Strategy: Computing Limits Algebraically

Suppose you want to compute  $\lim_{x \rightarrow a} \frac{f(x)}{g(x)}$ . Try plugging in  $a$  for  $x$ .

- $\frac{0}{0}$  Try to “simplify” (factor/cancel, clear denominators, multiply by conjugate, etc.).
- $\frac{\text{NOT } 0}{0}$  Compute the one-sided limits first. They should be  $\pm\infty$ .

1. Compute the following limits without graphing.

(a)  $\lim_{x \rightarrow -1} \frac{2x^2 + 3x + 1}{x^2 - 2x - 3}$

(b)  $\lim_{x \rightarrow 1^+} \frac{2 - x}{1 - x}$

(c)  $\lim_{x \rightarrow 0} \frac{x^2 + 2x}{x^3 + 3x^2}$

$$(d) \lim_{x \rightarrow 3} \frac{\frac{1}{x} - \frac{1}{3}}{x - 3}$$

$$(e) \lim_{h \rightarrow 0} \frac{(-3 + h)^2 - 9}{h}$$

$$(f) \lim_{x \rightarrow 16} \frac{4 - \sqrt{x}}{16x - x^2}$$