

Modern Algebra
MATH 325W – Spring 2015

Monday: Chapter 20-21: Cosets and Lagrange
Wednesday: Chapter 23: Normal Subgroups
Friday: Review for Exam 3

Week 13

HOMEWORK

Homework #22

due Tuesday, April 28

Ch. 20: #4(b)(c), 6(b)(c), 8(b)(c), 10, 15
Ch. 21: #2, 5, 6, 8

Homework #23

due Friday, May 1

Ch. 21: #20, 22, 46, 48
Ch. 23: #3, 6, 8
AP #1: Define $\text{SL}_2(\mathbb{R}) := \{A \in \text{GL}_2(\mathbb{R}) \mid \det A = 1\}$. Prove that $\text{SL}_2(\mathbb{R})$ is a normal subgroup of $\text{GL}_2(\mathbb{R})$ (with respect to matrix multiplication). You may freely use theorems from linear algebra.

WRITING ASSIGNMENTS

On writing assignments, part of your grade will reflect the quality of your *style*. Style includes everything from the basic mechanics of writing (complete, grammatically correct sentences with capitalization and proper punctuation) to the conventions of writing mathematics developed in Linear Algebra.

Writing Assignment #11

due Friday, May 01 ~~due Wednesday, April 29~~

Ch. 21: #28
AP #1: Let H be a subgroup of S_5 such that H contains a transposition, and $|H|$ is divisible by 5. Prove that $H = S_5$. *Hint: you can freely use Cauchy's theorem, see Proposition 22.9.*

Extra Credit: Define $\text{SL}_n(\mathbb{R}) := \{A \in \text{GL}_n(\mathbb{R}) \mid \det A = 1\}$, and note that $\text{SL}_n(\mathbb{R})$ is a subgroup of $\text{GL}_n(\mathbb{R})$. Concisely describe the left cosets of $\text{SL}_n(\mathbb{R})$ in $\text{GL}_n(\mathbb{R})$.