

Modern Algebra
MATH 325W – Spring 2015

Monday: Chapter 10: Algebraic Elements
Wednesday: Chapter 10: Algebraic Elements
Friday: Chapter 11: Eisenstein

Week 8

HOMEWORK

Homework #13

due Tuesday, March 10

Ch. 10: # 14, 20, 39, 42

Note: important information for #39 and #42 can be found right above #37.

Extra #1: Let $p(x) = x^3 - x + 1 \in \mathbb{Z}_3[x]$, and let r be a root of $p(x)$.

- (1) Prove that $p(x)$ is irreducible over \mathbb{Z}_3 .
- (2) Use Theorem 10.8 to describe $\mathbb{Z}_3(r)$.
- (3) How many elements are in the field $\mathbb{Z}_3(r)$?

Homework #14

due Friday, March 13

Ch. 11: #5–10, 14

WRITING ASSIGNMENTS

On writing assignments, part of your grade will reflect the quality of your *style*. Style includes everything from the basic mechanics of writing (complete, grammatically correct sentences with capitalization and proper punctuation) to the conventions of writing mathematics developed in Linear Algebra.

Writing Assignment #7

due Wednesday, March 11

Ch. 9: #25

Hint: modify the proof of 9.10. Let $I \subseteq \mathbb{Z}$ be an ideal. If $I = \{0\}$, then I is principal since in this case $I = (0)$. Now assume $I \neq \{0\}$. Let $S = \{a \mid a \in I \text{ and } a > 0\}$. Then the WOP applies to S (you explain why!), so S has a minimal element d . Then...

Also: Turn in a rewrite for one previous Writing Assignment (if you want). Make it beautiful!